

## Lecture 2

### Part E

***Selections -  
Laws of Logical Operators,  
Precedence of Logical Operators***

# Logical Law: Negation of Relational Operation

**Test Inputs:**  
 $i = 17, j = 3$   
 $i = -4, j = 13$

Relation	Negation	Equivalence
$i > j$	$!(i > j)$	$i \leq j$
$i \geq j$	$!(i \geq j)$	$i < j$
$i < j$	$!(i < j)$	$i \geq j$
$i \leq j$	$!(i \leq j)$	$i > j$

$17 \leq 3$

$!(i \leq j) \equiv i > j$

$!(i > j) \equiv i \leq j$

```

if (i > j) {
    /* Action 1 */
}
else { /* !(i > j) */
    /* Action 2 */
}
    
```

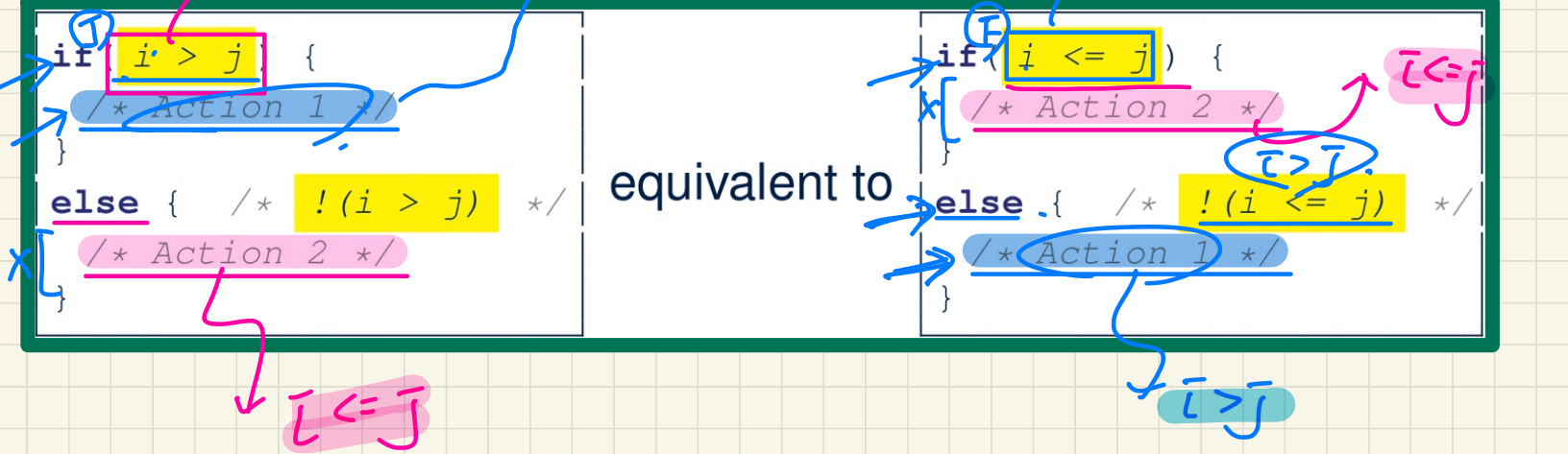
equivalent to

```

if (i <= j) {
    /* Action 2 */
}
else { /* !(i <= j) */
    /* Action 1 */
}
    
```

$i \leq j$

$i > j$



# Two-Way If-Stmt: Handling Errors

```
public class ComputeArea {
    public static void main(String[] args) {
        Scanner input = new Scanner(System.in);
        System.out.println("Enter a radius value:");
        double radius = input.nextDouble();
        final double PI = 3.14159;
        if (radius < 0) { /* condition of invalid inputs */
            System.out.println("Error: Negative radius value!");
        }
        else { /* implicit: !(radius < 0), or radius >= 0 */
            double area = radius * radius * PI;
            System.out.println("Area is " + area);
        }
        input.close();
    }
}
```

!(radius < 0)  
≡ radius >= 0

!(radius >= 0)  
"!"  
radius < 0

## Test Inputs:

radius = 9

radius = -5

Trace of both sides

-5 >= 0 (F)

```
public class ComputeArea2 {
    public static void main(String[] args) {
        Scanner input = new Scanner(System.in);
        System.out.println("Enter a radius value:");
        double radius = input.nextDouble();
        final double PI = 3.14159;
        if (radius >= 0) { /* condition of valid inputs */
            double area = radius * radius * PI;
            System.out.println("Area is " + area);
        }
        else { /* implicit: !(radius >= 0), or radius < 0 */
            System.out.println("Error: Negative radius value!");
        }
        input.close();
    }
}
```

# Logical Laws: DeMorgan

(T)

$B_1$	$B_2$	$!(B_1 \&\& B_2)$	$!B_1    !B_2$
true	true	false	false
true	false	true	true
false	true	true	true
false	false	true	true

DeMorgan for Conjunction

(!T) (F)

$B_1$	$B_2$	$!(B_1    B_2)$	$!B_1 \&\& !B_2$
true	true	false	false
true	false	false	false
false	true	false	false
false	false	true	true

DeMorgan for Disjunction

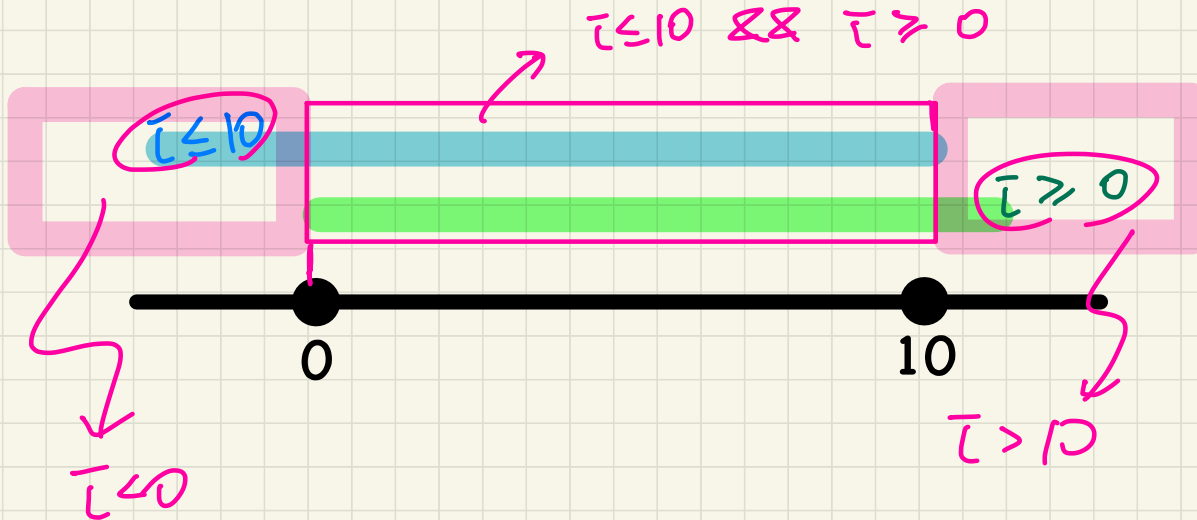
# DeMorgan Law of Conjunction: Example (1)

```
if (0 <= i && i <= 10) { /* Action 1 */ }  
else { /* Action 2 */ }
```

- When is Action 2 executed?

$i < 0 \ || \ i > 10$

$$\!(0 \leq \bar{i} \ \&\& \ \bar{i} \leq 10) \equiv \underline{\!(0 \leq \bar{i})} \ || \ \underline{\!(\bar{i} \leq 10)} \equiv 0 > \bar{i} \ || \ \bar{i} > 10$$



# DeMorgan Law of Conjunction: Example (2)

```
if(i < 0 && false) { /* Action 1 */ }  
else { /* Action 2 */ }
```

⤴ (F) - never executed

→ always executed.

- When is Action 1 executed? false
- When is Action 2 executed? true (i.e.,  $i \geq 0 \ || \ true$ )

$!(i < 0 \ \&\& \ \underline{false})$   
||  
 $!(i < 0) \ || \ \underline{!(false)}$   
||  
 $i \geq 0 \ \underline{=} \ \underline{i}$   
||  
 $(T)$

$i < 0 \ \&\& \ \underline{false}$   
↓  
 $(F)$

# DeMorgan Law of Conjunction: Example (3)

```
if (i < 0 && i > 10) { /* Action 1 */ }  
else { /* Action 2 */ }
```

never executed.

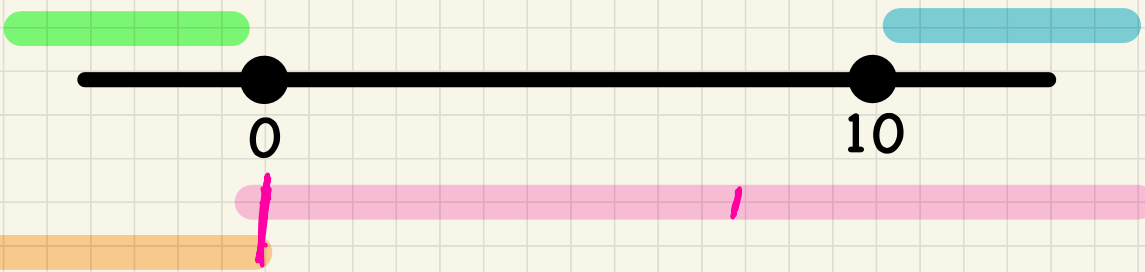
always executed.

- When is *Action 1* executed? false
- When is *Action 2* executed? *true* (i.e.,  $i \geq 0 \mid\mid i \leq 10$ )



$$\begin{aligned} & \rightarrow \neg ( \neg i < 0 \ \&\& \ \neg i > 10 ) \\ & \equiv \neg ( \neg i < 0 ) \ \vee \ \neg ( \neg i > 10 ) \equiv \boxed{ i \geq 0 \ \vee \ i \leq 10 } \end{aligned}$$

(T)



# DeMorgan Law of Disjunction: Example (1)

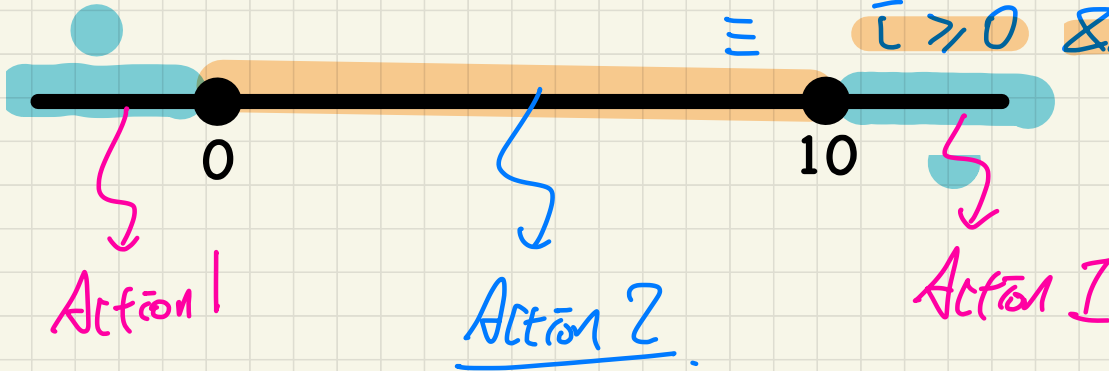
```
if( $i < 0 \ || \ i > 10$ ) { /* Action 1 */ }  
else { /* Action 2 */ }
```

- When is Action 2 executed?

$0 \leq i \ \&\& \ i \leq 10$

$$\underline{\underline{\neg(i < 0 \ || \ i > 10)}} \equiv \underline{\underline{\neg(i < 0)}} \ \&\& \ \underline{\underline{\neg(i > 10)}}$$

$$\equiv \underline{\underline{i \geq 0}} \ \&\& \ \underline{\underline{i \leq 10}}$$





# DeMorgan Law of Disjunction: Example (2)

```
if (i < 0 || true) { /* Action 1 */ }  
else { /* Action 2 */ }
```

always executed

never executed

- When is *Action 1* executed? *true*
- When is *Action 2* executed? *false* (i.e.,  $i \geq 0 \ \&\& \ \text{false}$ )

$!(i < 0 \ || \ \text{true})$

De Morgan

EXERCISE

$i < 0 \ || \ \underline{\underline{\text{true}}}$

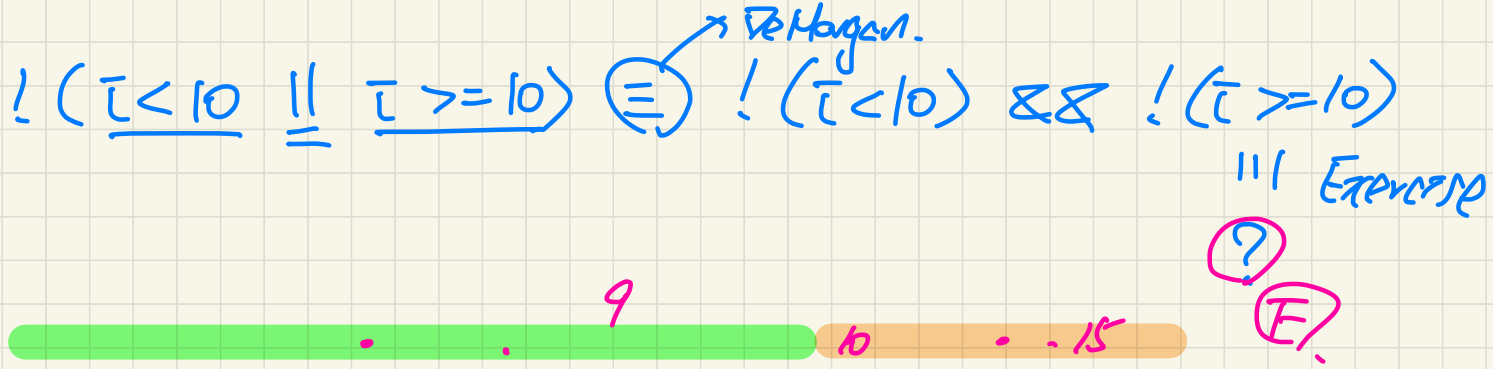
(F)

(T)

# DeMorgan Law of Disjunction: Example (3)

```
if (i < 10 || i >= 10) { /* Action 1 */ }  
else { /* Action 2 */ }
```

- When is *Action 1* executed? true
- When is *Action 2* executed? false (i.e.,  $i \geq 10 \ \&\& \ i < 10$ )



# Precedence of Logical Operators

boolean p = true;  
 boolean q = true;  
 boolean r = false;

!  
 &&  
 ||

⊗ has higher than precedence  
 evaluated first

✓  
 p || (q && r)

✓  
 (p || q) && r

✓ ✓  
 p || (q && r)

✓  
 T || (T && F)  
 F

✓  
 (T || T) && F  
 T

✓ ✓  
 p || q && r.  
 (p || q) && r

① = ② ≠ ③

⊗

EXERCISE  
 Find p, q, r showing

① !p || q && r ≡ ② (!p) || (q && r)  
 ② and ③ may evaluate to different results.

## Lecture 2

### Part F

***Selections -  
Two-Way vs. Multi-Ways If-Statements,  
Nested If-Statements***

## Two-Way If-Statement without else Part

<sup>-23</sup> <sup>ⓐ</sup> <sup>ⓑ</sup>

```
if (radius >= 0) {  
    area = radius * radius * PI;  
    System.out.println("Area for the circle of is " + area);  
}
```

Console

Area for circle is . -

<sup>-23</sup> <sup>ⓐ</sup>

```
if (radius >= 0) {  
    area = radius * radius * PI;  
    System.out.println("Area for the circle of is " + area);  
}  
else {  
    /* Do nothing. */  
}
```

Console

Area for circle is . -

Test Inputs:

radius = 10

radius = -23

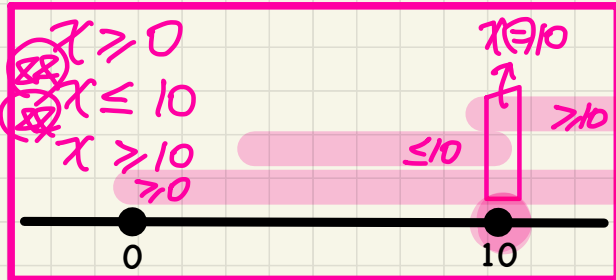
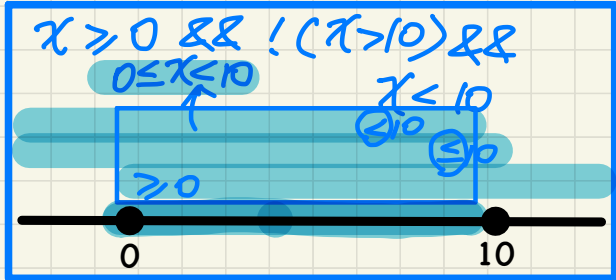
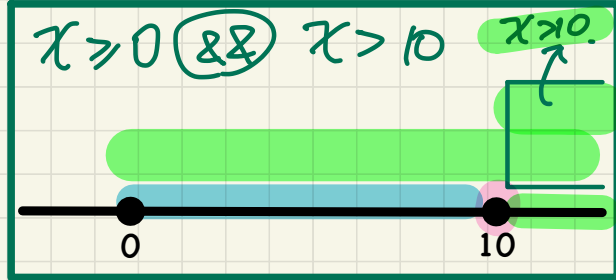
Console

Console

# Compound If-Statement: Implicit Conditions

```
1 int x = input.nextInt();
2 int y = 0;
3 if (x >= 0) {
4     System.out.println("x is positive");
5     if (x > 10) { y = x * 2; }
6     else if (x < 10) { y = x % 2; }
7     else { y = x * x; }
8 }
9 else { /* x < 0 */
10     System.out.println("x is negative");
11     if (x < -5) { y = -x; }
12 }
```

single if-statement



# Compound If-Statement: Tracing

```
1  int x = input.nextInt();
2  int y = 0;
3  if (x >= 0) {
4      System.out.println("x is positive");
5      if (x > 10) { x * y = x * 2; }
6      else if (x < 10) { y = x % 2; }
7      else { y = x * x; }
8  }
9  else { /* x < 0 */
10     System.out.println("x is negative");
11     if (x < -5) { y = -x; }
12 }
```

## Test Inputs:

x = 5

x = 10

x = -2

Exercise:

Trace on  
paper and

Debugger.

0

10

# Multi-Way If-Statement with else Part

71 (F)

```
if (score >= 80.0) {  
    System.out.println("A");  
}  
else if (score >= 70.0) {  
    System.out.println("B");  
}  
else if (score >= 60.0) {  
    System.out.println("C");  
}  
else {  
    System.out.println("F");  
}
```

71 (F)

```
if (score >= 80.0) {  
    System.out.println("A");  
}  
else if (score >= 70.0) {  
    System.out.println("B");  
}  
else if (score >= 60.0) {  
    System.out.println("C");  
}  
else {  
    System.out.println("F");  
}
```

≡

```
if (score >= 80.0) {  
    System.out.println("A");  
}  
else if (score >= 70.0) {  
    System.out.println("B");  
}  
else if (score >= 60.0) {  
    System.out.println("C");  
}  
else {  
    System.out.println("F");  
}
```

## Test Inputs:

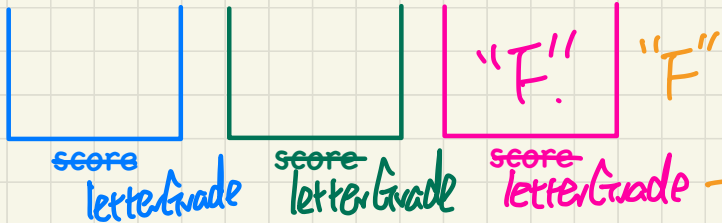
score = 83

score = 71

score = 59



# Multi-Way If-Statement without else Part



```
String letterGrade = "F";  
if (score >= 80.0) {  
    letterGrade = "A";  
}  
else if (score >= 70.0) {  
    letterGrade = "B";  
}  
else if (score >= 60.0) {  
    letterGrade = "C";  
}
```

```
String letterGrade = "F";  
if (score >= 80.0) {  
    letterGrade = "A";  
}  
else {  
    if (score >= 70.0) {  
        letterGrade = "B";  
    }  
    else {  
        if (score >= 60.0) {  
            letterGrade = "C";  
        }  
        else {  
            /* do nothing */  
        }  
    }  
}
```

**Test Inputs:**  
score = 83  
score = 71  
score = 59

## Lecture 2

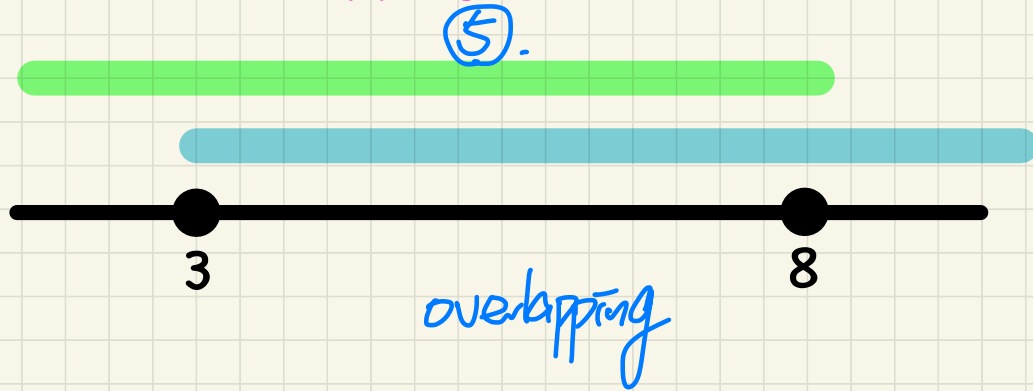
### Part G

***Selections -  
Overlapping vs. Disjoint Conditions,  
Single If-Stmt vs. Multiple If-Stmts***

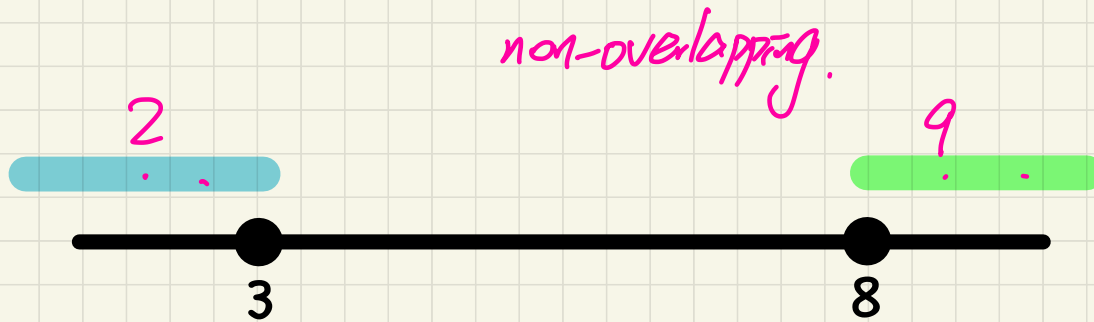
# Overlapping vs. Non-Overlapping Intervals

→ disjoint.

$i \geq 3$   
 $i \leq 8$



$i \leq 3$   
 $i \geq 8$



# Single If-Stmt vs. Multiple If-Stmts: Overlapping Conditions

- single vs. multiple  
- overlapping.

```
int i = 5;  
if (i >= 3) {System.out.println("i is >= 3");}  
else if (i <= 8) {System.out.println("i is <= 8");}
```

## Console

i ↗ >= 3

*independent if-stmts.*

```
int i = 5;  
if (i >= 3) {System.out.println("i is >= 3");}  
if (i <= 8) {System.out.println("i is <= 8");}
```

## Console

i ↗ >= 3  
i ↗ <= 8

## Single If-Stmt vs. Multiple If-Stmts: Non-Overlapping Conditions

```
int i = 2;
```

```
if (i <= 3) {System.out.println("i is <= 3");}  
else if (i >= 8) {System.out.println("i is >= 8");}
```

### Console

i ↗ <= 3

```
int i = 2;
```

```
if (i <= 3) {System.out.println("i is <= 3");}  
if (i >= 8) {System.out.println("i is >= 8");}
```

### Console

i ↗ <= 3

# Common Error: Multiple If-Statements with Overlapping Conditions

```
if (marks >= 80) {  
    System.out.println("A");  
}  
if (marks >= 70) {  
    System.out.println("B");  
}  
if (marks >= 60) {  
    System.out.println("C");  
}  
else {  
    System.out.println("F");  
}
```

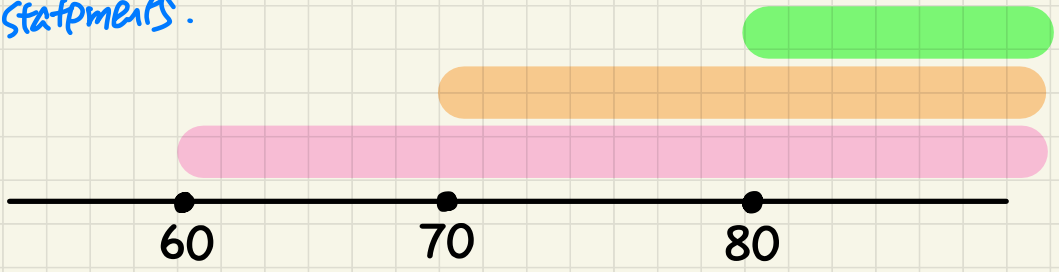
Annotations: Red box around the entire code block. Blue boxes around each if statement. Handwritten '84' above each if condition. Handwritten 'T' in a circle next to each if condition. A red 'X' is next to the else block. A red arrow points to the first if statement.

```
if (marks >= 80) {  
    System.out.println("A");  
}  
else if (marks >= 70) {  
    System.out.println("B");  
}  
else if (marks >= 60) {  
    System.out.println("C");  
}  
else {  
    System.out.println("F");  
}
```

Annotations: Blue box around the entire code block. Handwritten '84' above the first if condition. Handwritten 'Correct' in green with an arrow pointing to the first if statement. Handwritten 'A!' in a pink circle next to the first if statement. A blue arrow points to the else block with the text 'single if-statement'.

A  
B  
C

3 if-statements.



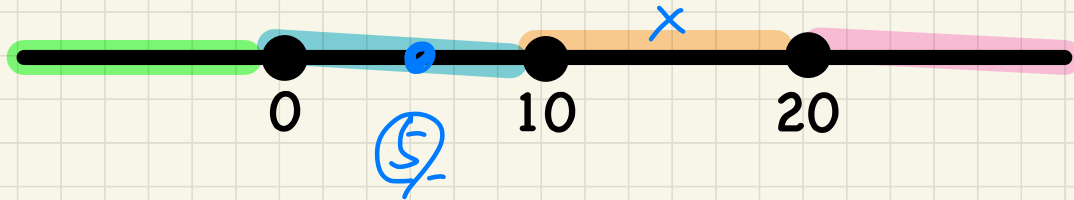
**Test Inputs:**  
marks = 84

# Overlapping Conditions: Exercise (1)

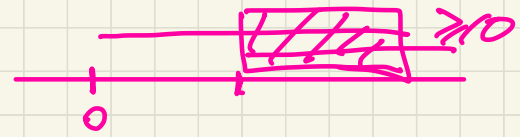
Does this program always print exactly one line?

```
if (x < 0) { println("x < 0"); }
if (0 <= x && x < 10) { println("0 <= x < 10"); }
if (10 <= x && x < 20) { println("10 <= x < 20"); }
if (x >= 20) { println("x >= 20"); }
```

disjoint.  
no value can satisfy more than one of them  
⇒ only one if-stmt's body of code is executed.



# Overlapping Conditions: Exercises (2, 3)



Does this program always print exactly one line?

```
if(x < 0) { println("x < 0"); }  
else if(0 <= x && x < 10) { println("0 <= x < 10"); }  
else if(10 <= x && x < 20) { println("10 <= x < 20"); }  
else if(x >= 20) { println("x >= 20"); }
```

→ single if statement ⇒ exactly one branch is executed

This simplified version is equivalent:

```
if(x < 0) { println("x < 0"); }  
else if(x < 10) { println("0 <= x < 10"); }  
else if(x < 20) { println("10 <= x < 20"); }  
else { println("x >= 20"); }
```

$$\begin{aligned} & \rightarrow \underline{!(x < 0)} \ \&\& \ x < 10 \\ & \equiv \ x \geq 0 \ \&\& \ x < 10 \end{aligned}$$

$$\begin{aligned} & \underline{!(x < 0)} \ \&\& \ \underline{!(x < 10)} \ \&\& \ x < 20 \\ & \equiv \ x \geq 0 \ \&\& \ x \geq 10 \ \&\& \ x < 20 \end{aligned}$$



# Lecture 2

## Part H

### ***Selections - Scope of Variables***

## Scope of Variables: Method

```
public static void main(String[] args) {  
    int i = input.nextInt();  
    System.out.println("i is " + i);  
    if (i > 0) {  
        : i = i * 3; /* both use and re-assignment, why? */  
    }  
    else {  
        : i = i * -3; /* both use and re-assignment, why? */  
    }  
    System.out.println("3 * i is " + i);  
}
```

## Scope of Variables: Branches

```
public static void main(String[] args) {  
    int i = input.nextInt();  
    if (i > 0) {  
        int j = i * 3; /* a new variable j */  
        if (j > 10) { ... }  
    }  
    else {  
        int j = i * -3; /* a new variable also called j */  
        if (j < 10) { ... }  
    }  
}
```

## Scope of Variables: Use of Variables from Other Branches

```
public static void main(String[] args) {  
    int i = input.nextInt();  
    if (i > 0) {  
        int j = i * 3; /* a new variable j */  
        if (j > 10) { ... }  
    }  
    else {  
        int k = i * -3; /* a new variable also called j */  
        if (j < k) { ... }  
    }  
}
```

The code illustrates variable scope in a conditional branch. The variable `j` is declared in the `if` branch and is used in the `else` branch. A pink box highlights the `int j = i * 3;` line in the `if` branch, and an orange box highlights the `int k = i * -3;` line in the `else` branch. A blue arrow points to the `int i = input.nextInt();` line. A pink 'X' is placed below the `if (j < k)` line, indicating that the variable `j` is not in scope in the `else` branch, which is why the code is marked with a red 'X'.

# Scope of Variables: Use of Variables Outside If-Stmt

```
public static void main(String[] args) {  
    int i = input.nextInt();  
    if (i > 0) {  
        int j = i * 3; /* a new variable j */  
        if (j > 10) { ... }  
    }  
    else {  
        int j = i * -3; /* a new variable also called j */  
        if (j < 10) { ... }  
    }  
    System.out.println(i * j is " + i * j);  
}
```

outside  
scopes of  
[ ] and  
[ ]

# Scope of Variables: Method Parameters & Return Values

```
1 public class SumApp {  
2     public static void main(String[] args) {  
3         Scanner input = new Scanner(System.in);  
4         int i = input.nextInt();  
5         int j = input.nextInt();  
6         int k = Utilities.getSum(j, j);  
7         System.out.println(k);  
8     }  
}
```

conceptually:

→ int k = result;  
↳ what Java run time does

```
public class Utilities {  
    public static int getSum(int X, int X) {  
        int result = X + X;  
        return result;  
    }  
}
```

but you can not write this